

## General:

|                          |   |
|--------------------------|---|
| Reflexive Property       | A quantity is congruent (equal) to itself. $a = a$  |
| Symmetric Property       | If $a = b$ , then $b = a$ .   |
| Transitive Property      | If $a = b$ and $b = c$ , then $a = c$ .   |
| Addition Postulate       | If equal quantities are added to equal quantities, the sums are equal.  |
| Subtraction Postulate    | If equal quantities are subtracted from equal quantities, the differences are equal.  |
| Multiplication Postulate | If equal quantities are multiplied by equal quantities, the products are equal. (also Doubles of equal quantities are equal.)   |
| Division Postulate       | If equal quantities are divided by equal nonzero quantities, the quotients are equal. (also Halves of equal quantities are equal.)  |
| Substitution Postulate   | A quantity may be substituted for its equal in any expression.  |
| Partition Postulate      | The whole is equal to the sum of its parts.<br>Also: <b>Betweenness of Points:</b> $AB + BC = AC$<br><b>Angle Addition Postulate:</b> $m\angle ABC + m\angle CBD = m\angle ABD$ |
| Construction             | Two points determine a straight line.   |
| Construction             | From a given point on (or not on) a line, one and only one perpendicular can be drawn to the line.  |

## Angles:

|   |   |
|---|---|
| Right Angles                                | All right angles are congruent.   |
| Straight Angles                             | All straight angles are congruent.  |
| Congruent Supplements                       | Supplements of the same angle, or congruent angles, are congruent.  |
| Congruent Complements                       | Complements of the same angle, or congruent angles, are congruent.  |
| Linear Pair                                 | If two angles form a linear pair, they are supplementary.   |
| Vertical Angles                             | Vertical angles are congruent.  |
| Triangle Sum                                | The sum of the interior angles of a triangle is $180^\circ$ .   |
| Exterior Angle                              | The measure of an exterior angle of a triangle is equal to the sum of the measures of the two non-adjacent interior angles.<br>The measure of an exterior angle of a triangle is greater than either non-adjacent interior angle. |
| Base Angle Theorem<br>(Isosceles Triangle)  | If two sides of a triangle are congruent, the angles opposite these sides are congruent.  |
| Base Angle Converse<br>(Isosceles Triangle) | If two angles of a triangle are congruent, the sides opposite these angles are congruent.   |

## Triangles:

|   |   |
|---|---|
| Side-Side-Side ( <b>SSS</b> )<br>Congruence                 | If three sides of one triangle are congruent to three sides of another triangle, then the triangles are congruent.  |
| Side-Angle-Side ( <b>SAS</b> )<br>Congruence                | If two sides and the included angle of one triangle are congruent to the corresponding parts of another triangle, the triangles are congruent.  |
| Angle-Side-Angle ( <b>ASA</b> )<br>Congruence               | If two angles and the included side of one triangle are congruent to the corresponding parts of another triangle, the triangles are congruent.  |
| Angle-Angle-Side ( <b>AAS</b> )<br>Congruence               | If two angles and the non-included side of one triangle are congruent to the corresponding parts of another triangle, the triangles are congruent.  |
| Hypotenuse-Leg ( <b>HL</b> )<br>Congruence (right triangle) | If the hypotenuse and leg of one right triangle are congruent to the corresponding parts of another right triangle, the two right triangles are congruent.                                |
| <b>CPCTC</b>  | Corresponding parts of congruent triangles are congruent.   |
| Angle-Angle ( <b>AA</b> )<br>Similarity                     | If two angles of one triangle are congruent to two angles of another triangle, the triangles are <b>similar</b> .   |
| <b>SSS</b> for Similarity                                   | If the three sets of corresponding sides of two triangles are in proportion, the triangles are similar.   |
| <b>SAS</b> for Similarity                                   | If an angle of one triangle is congruent to the corresponding angle of another triangle and the lengths of the sides including these angles are in proportion, the triangles are similar. |
| Side Proportionality  | If two triangles are <b>similar</b> , the corresponding sides are in proportion.  |
| Mid-segment Theorem<br>(also called mid-line)               | The segment connecting the midpoints of two sides of a triangle is <b>parallel</b> to the third side and is half as long.   |
| Sum of Two Sides  | The sum of the lengths of any two sides of a triangle must be greater than the third side   |
| Longest Side  | In a triangle, the longest side is across from the largest angle.<br>In a triangle, the largest angle is across from the longest side.  |
| Altitude Rule   | The <b>altitude</b> to the hypotenuse of a right triangle is the mean proportional between the segments into which it divides the hypotenuse.   |
| Leg Rule  | Each <b>leg</b> of a right triangle is the mean proportional between the hypotenuse and the projection of the leg on the hypotenuse.  |

## Parallels:

|                                    |  |
|------------------------------------|--|
| Corresponding Angles               | If two <b>parallel</b> lines are cut by a transversal, then the pairs of corresponding angles are congruent.   |
| Corresponding Angles Converse      | If two lines are cut by a transversal and the corresponding angles are congruent, the lines are <b>parallel</b> .                                    |
| Alternate Interior Angles          | If two <b>parallel</b> lines are cut by a transversal, then the alternate interior angles are congruent.   |
| Alternate Exterior Angles          | If two <b>parallel</b> lines are cut by a transversal, then the alternate exterior angles are congruent.   |
| Interiors on Same Side             | If two <b>parallel</b> lines are cut by a transversal, the interior angles on the same side of the transversal are supplementary.                    |
| Alternate Interior Angles Converse | If two lines are cut by a transversal and the alternate interior angles are congruent, the lines are <b>parallel</b> .                               |
| Alternate Exterior Angles Converse | If two lines are cut by a transversal and the alternate exterior angles are congruent, the lines are <b>parallel</b> .                               |
| Interiors on Same Side Converse    | If two lines are cut by a transversal and the interior angles on the same side of the transversal are supplementary, the lines are <b>parallel</b> . |

## Quadrilaterals:

|                         |                        |   |
|-------------------------|------------------------|---|
| Parallelograms          | <b>About Sides</b>     | <ul style="list-style-type: none"> <li>* If a quadrilateral is a parallelogram, the opposite sides are parallel.</li> <li>* If a quadrilateral is a parallelogram, the opposite sides are congruent.</li> </ul>   |
|                         | <b>About Angles</b>    | <ul style="list-style-type: none"> <li>* If a quadrilateral is a parallelogram, the opposite angles are congruent.</li> <li>* If a quadrilateral is a parallelogram, the consecutive angles are supplementary.</li> </ul>   |
|                         | <b>About Diagonals</b> | <ul style="list-style-type: none"> <li>* If a quadrilateral is a parallelogram, the diagonals bisect each other.</li> <li>* If a quadrilateral is a parallelogram, the diagonals form two congruent triangles.</li> </ul>   |
| Parallelogram Converses | <b>About Sides</b>     | <ul style="list-style-type: none"> <li>* If both pairs of opposite sides of a quadrilateral are parallel, the quadrilateral is a parallelogram.</li> <li>* If both pairs of opposite sides of a quadrilateral are congruent, the quadrilateral is a parallelogram.</li> </ul> |
|                         | <b>About Angles</b>    | <ul style="list-style-type: none"> <li>* If both pairs of opposite angles of a quadrilateral are congruent, the quadrilateral is a parallelogram.</li> <li>* If the consecutive angles of a quadrilateral are supplementary, the quadrilateral is a parallelogram.</li> </ul> |
|                         | <b>About Diagonals</b> | <ul style="list-style-type: none"> <li>* If the diagonals of a quadrilateral bisect each other, the quadrilateral is a parallelogram.</li> <li>* If the diagonals of a quadrilateral form two congruent triangles, the quadrilateral is a parallelogram.</li> </ul>           |

|                     |   |
|---------------------|---|
| Parallelogram       | If one pair of sides of a quadrilateral is BOTH parallel and congruent, the quadrilateral is a parallelogram. |
| Rectangle           | If a parallelogram has one right angle it is a rectangle  |
|                     | A parallelogram is a rectangle if and only if its diagonals are congruent.                                    |
|                     | A rectangle is a parallelogram with four right angles.  |
| Rhombus             | A rhombus is a parallelogram with four congruent sides.   |
|                     | If a parallelogram has two consecutive sides congruent, it is a rhombus.                                      |
|                     | A parallelogram is a rhombus if and only if each diagonal bisects a pair of opposite angles.                  |
|                     | A parallelogram is a rhombus if and only if the diagonals are perpendicular.                                  |
| Square              | A square is a parallelogram with four congruent sides and four right angles.                                  |
|                     | A quadrilateral is a square if and only if it is a rhombus and a rectangle.                                   |
| Trapezoid           | A trapezoid is a quadrilateral with exactly one pair of parallel sides.                                       |
| Isosceles Trapezoid | An isosceles trapezoid is a trapezoid with congruent legs.  |
|                     | A trapezoid is isosceles if and only if the base angles are congruent   |
|                     | A trapezoid is isosceles if and only if the diagonals are congruent   |
|                     | If a trapezoid is isosceles, the opposite angles are supplementary.   |

## Circles:

|          |   |
|----------|---|
| Radius   | In a circle, a radius perpendicular to a chord bisects the chord and the arc.                           |
|          | In a circle, a radius that bisects a chord is perpendicular to the chord.                               |
|          | In a circle, the perpendicular bisector of a chord passes through the center of the circle.             |
|          | If a line is tangent to a circle, it is perpendicular to the radius drawn to the point of tangency.     |
| Chords   | In a circle, or congruent circles, congruent chords are equidistant from the center. (and converse)     |
|          | In a circle, or congruent circles, congruent chords have congruent arcs. (and converse)                 |
|          | In a circle, parallel chords intercept congruent arcs   |
|          | In the same circle, or congruent circles, congruent central angles have congruent chords (and converse) |
| Tangents | Tangent segments to a circle from the same external point are congruent                                 |
| Arcs     | In the same circle, or congruent circles, congruent central angles have congruent arcs. (and converse)  |
| Angles   | An angle inscribed in a semi-circle is a right angle.   |
|          | In a circle, inscribed angles that intercept the same arc are congruent.                                |
|          | The opposite angles in a cyclic quadrilateral are supplementary   |
|          | In a circle, or congruent circles, congruent central angles have congruent arcs.                        |